

# 10th Exercise sheet for Advanced Algorithmics, SS 15

**Hand In:** Until Wednesday, 01.07.2015, 12:00am, in lecture, exercise sessions, hand-in box in stairwell 48-6 or via email.

## Problem 27

Modify the algorithm CONTRACTION as follows. Instead of randomly choosing an edge and contracting, randomly choose two vertices  $x, y$  and identify them into one vertex.

Prove that for some (infinite class of) graphs, the probability that this modified algorithm finds a minimal cut is exponentially small in the number of vertices  $n$ .

## Problem 28

- Assume you have access to an oracle that can determine in polynomial time and for arbitrary graphs which size a minimal VERTEX COVER has. How can you use it to construct a minimal VERTEX COVER in polynomial time?
- Does the approach from a) also work for factorising integers? Why (not)?
- Argue why problems for which the method from a) is effective are often amenable to branch-&-bound algorithms.

## Problem 29

Give a (deterministic) 2-approximation for MAXIMUM SUBGRAPH (cf. Problem 19).